# Mark Scheme (Results) January 2010 

GCE

## GCE Further Pure Mathematics FP1 (6667/ 01)

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## 6667 Further Pure Mathematics FP1

## Mark Scheme

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q1 |  | M1 <br> A1 A1 <br> (3) |
|  | (b) $\left\|\frac{z_{1}}{z_{2}}\right\|=\sqrt{(-3)^{2}+5^{2}}=\sqrt{34} \quad$ (or awrt 5.83) | M1 A1ft <br> (2) |
|  | $\text { (c) } \begin{aligned} \tan \alpha & =-\frac{5}{3} \text { or } \frac{5}{3} \\ \arg \frac{z_{1}}{z_{2}} & =\pi-1.03 \ldots=2.11 \end{aligned}$ | M1 <br> A1 <br> (2) [7] |
|  | Notes <br> (a) $\times \frac{1+\mathrm{i}}{1+\mathrm{i}}$ and attempt to multiply out for M1 <br> -3 for first A1, +5 i for second A1 <br> (b) Square root required without i for M1 <br> $\frac{\left\|z_{1}\right\|}{\left\|z_{2}\right\|}$ award M1 for attempt at Pythagoras for both numerator and denominator <br> (c) $\tan$ or $\tan ^{-1}, \pm \frac{5}{3}$ or $\pm \frac{3}{5}$ seen with their 3 and 5 award M1 <br> 2.11 correct answer only award A1 |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q2 | (a) $\mathrm{f}(1.3)=-1.439$ and $\mathrm{f}(1.4)=0.268$ (allow awrt) | B1 <br> (1) |
|  | (b) $\mathrm{f}(1.35)<0(-0.568 \ldots)$ $\Rightarrow$ $1.35<\alpha<1.4$ <br> $\mathrm{f}(1.375)<0(-0.146 \ldots)$ $\Rightarrow$ $1.375<\alpha<1.4$ | M1 A1 A1 |
|  | $\begin{aligned} \text { (c) } \mathrm{f}^{\prime}(x) & =6 x+22 x^{-3} \\ x_{1} & =x_{0}-\frac{\mathrm{f}\left(x_{0}\right)}{\mathrm{f}^{\prime}\left(x_{0}\right)}=1.4-\frac{0.268}{16.417}, \quad=1.384 \end{aligned}$ | M1 A1 <br> M1 A1, A1 <br> (5) <br> [9] |
|  | Notes <br> (a) Both answers required for B1. Accept anything that rounds to 3dp values above. <br> (b) $\mathrm{f}(1.35)$ or awrt -0.6 M 1 <br> ( $\mathrm{f}(1.35$ ) and awrt -0.6 ) AND ( $\mathrm{f}(1.375$ ) and awrt -0.1 ) for first A1 <br> $1.375<\alpha<1.4$ or expression using brackets or equivalent in words for second A1 <br> (c) One term correct for M1, both correct for A1 <br> Correct formula seen or implied and attempt to substitute for M1 awrt 16.4 for second A1 which can be implied by correct final answer awrt 1.384 correct answer only A1 |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q3 | For $n=1: u_{1}=2, u_{1}=5^{0}+1=2$ <br> Assume true for $n=k$ : $u_{k+1}=5 u_{k}-4=5\left(5^{k-1}+1\right)-4=5^{k}+5-4=5^{k}+1$ <br> $\therefore$ True for $n=k+1$ if true for $n=k$. <br> True for $n=1$, <br> $\therefore$ true for all $n$. | B1 <br> M1 A1 <br> A1 cso |
|  | Notes <br> Accept $u_{1}=1+1=2$ or above B1 $5\left(5^{k-1}+1\right)-4 \text { seen award M1 }$ <br> $5^{k}+1$ or $5^{(k+1)-1}+1$ award first A1 <br> All three elements stated somewhere in the solution award final A1 |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q4 | (a) $(3,0)$ cao | B1 <br> (1) |
|  | (b) $P: \quad x=\frac{1}{3} \Rightarrow \quad y=2$ <br> $A$ and $B$ lie on $x=-3$ <br> $P B=P S \quad$ or a correct method to find both $P B$ and $P S$ $\text { Perimeter }=6+2+3 \frac{1}{3}+3 \frac{1}{3}=14 \frac{2}{3}$ | B1 <br> B1 <br> M1 <br> M1 A1 <br> (5) <br> [6] |
|  | Notes <br> (b) Both B marks can be implied by correct diagram with lengths labelled or coordinates of vertices stated. <br> Second M1 for their four values added together. <br> $14 \frac{2}{3}$ or awrt 14.7 for final A1 |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q5 | (a) $\operatorname{det} \mathbf{A}=a(a+4)-(-5 \times 2)=a^{2}+4 a+10$ | M1 A1 |
|  | (b) $a^{2}+4 a+10=(a+2)^{2}+6$ <br> Positive for all values of $a$, so $\mathbf{A}$ is non-singular | M1 A1ft A1cso |
|  | (c) $\mathbf{A}^{-1}=\frac{1}{10}\left(\begin{array}{cc}4 & 5 \\ -2 & 0\end{array}\right)$ <br> B1 for $\frac{1}{10}$ | B1 M1 A1 <br> (3) <br> [8] |
|  | Notes <br> (a) Correct use of $a d-b c$ for M1 <br> (b) Attempt to complete square for M1 <br> Alt 1 <br> Attempt to establish turning point (e.g. calculus, graph) M1 <br> Minimum value 6 for A1ft <br> Positive for all values of $a$, so $\mathbf{A}$ is non-singular for A1 cso <br> Alt 2 <br> Attempt at $b^{2}-4 a c$ for M1. Can be part of quadratic formula <br> Their correct -24 for first A1 <br> No real roots or equivalent, so $\mathbf{A}$ is non-singular for final A1cso <br> (c) Swap leading diagonal, and change sign of other diagonal, with numbers or $a$ for M1 <br> Correct matrix independent of 'their $\frac{1}{10}$ award' final A1 |  |



| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q7 | $\begin{align*} \text { (a) } \begin{aligned} y & =\frac{c^{2}}{x} \quad \begin{aligned} \frac{\mathrm{d} y}{\mathrm{~d} x} & =-c^{2} x^{-2} \\ \frac{\mathrm{~d} y}{\mathrm{~d} x} & =-\frac{c^{2}}{(c t)^{2}}=-\frac{1}{t^{2}} \\ y-\frac{c}{t}=-\frac{1}{t^{2}}(x-c t) & \Rightarrow \quad t^{2} y+x=2 c t \end{aligned} \quad \text { without } x \text { or } y \end{aligned} \quad \text {, } \quad \text { (*) } \end{align*}$ | B1 <br> M1 <br> M1 A1cso <br> (4) |
|  | (b) Substitute $(15 c,-c):-c t^{2}+15 c=2 c t$ $\begin{gathered} t^{2}+2 t-15=0 \\ (t+5)(t-3)=0 \quad \Rightarrow \quad t=-5 \quad t=3 \end{gathered}$ <br> Points are $\left(-5 c,-\frac{c}{5}\right)$ and $\left(3 c, \frac{c}{3}\right)$ | M1 <br> A1 <br> M1 A1 <br> A1 <br> (5) <br> [9] |
|  | Notes <br> (a) Use of $y-y_{1}=m\left(x-x_{1}\right)$ where $m$ is their gradient expression in terms of $c$ and / or $t$ only for second M1. Accept $y=m x+k$ and attempt to find $k$ for second M1. <br> (b) Correct absolute factors for their constant for second M1. <br> Accept correct use of quadratic formula for second M1. <br> Alternatives: <br> (a) $\begin{array}{ll} \frac{\mathrm{d} x}{\mathrm{~d} t}=c & \text { and } \frac{\mathrm{d} y}{\mathrm{~d} t}=-c t^{-2} \end{array} \text { B1 } \quad \begin{array}{ll} \frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{\mathrm{d} y}{\mathrm{~d} t} \div \frac{\mathrm{d} x}{\mathrm{~d} t}=-\frac{1}{t^{2}} & \text { M1, then as in main scheme. } \end{array}$ <br> (a) $\begin{aligned} & y+x \frac{\mathrm{~d} y}{\mathrm{~d} x}=0 \\ & \frac{\mathrm{~d} y}{\mathrm{~d} x}=-\frac{y}{x}=-\frac{1}{t^{2}} \end{aligned}$ B1 <br> M1, then as in main scheme. |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q8 | (a) $\sum_{r=1}^{1} r^{3}=1^{3}=1$ and $\frac{1}{4} \times 1^{2} \times 2^{2}=1$ <br> Assume true for $n=k$ : $\begin{aligned} & \sum_{r=1}^{k+1} r^{3}=\frac{1}{4} k^{2}(k+1)^{2}+(k+1)^{3} \\ & \frac{1}{4}(k+1)^{2}\left[k^{2}+4(k+1)\right]=\frac{1}{4}(k+1)^{2}(k+2)^{2} \end{aligned}$ <br> $\therefore$ True for $n=k+1$ if true for $n=k$. <br> True for $n=1$, <br> $\therefore$ true for all $n$. | B1 <br> B1 <br> M1 A1 <br> A1cso |
|  | $\text { (b) } \begin{align*} & \sum r^{3}+3 \sum r+\sum 2=\frac{1}{4} n^{2}(n+1)^{2}+3\left(\frac{1}{2} n(n+1)\right),+2 n  \tag{5}\\ & =\frac{1}{4} n\left[n(n+1)^{2}+6(n+1)+8\right] \\ & =\frac{1}{4} n\left[n^{3}+2 n^{2}+7 n+14\right]=\frac{1}{4} n(n+2)\left(n^{2}+7\right) \tag{*} \end{align*}$ | B1, B1 <br> M1 <br> A1 A1cso <br> (5) |
|  | $\begin{aligned} & \text { (c) } \sum_{15}^{25}=\sum_{1}^{25}-\sum_{1}^{14} \quad \quad \text { with attempt to sub in answer to part (b) } \\ & =\frac{1}{4}(25 \times 27 \times 632)-\frac{1}{4}(14 \times 16 \times 203)=106650-11368=95282 \end{aligned}$ | M1 <br> A1 <br> (2) <br> [12] |
|  | Notes <br> (a) Correct method to identify $(k+1)^{2}$ as a factor award M1 $\frac{1}{4}(k+1)^{2}(k+2)^{2}$ award first A1 <br> All three elements stated somewhere in the solution award final A1 <br> (b) Attempt to factorise by $n$ for M1 <br> $\frac{1}{4}$ and $n^{3}+2 n^{2}+7 n+14$ for first A1 <br> (c) no working $0 / 2$ |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q9 | (a) $45^{\circ}$ or $\frac{\pi}{4}$ rotation (anticlockwise), about the origin | B1, B1 (2) |
|  | (b) $\left(\begin{array}{cc}\frac{1}{\sqrt{ } 2} & -\frac{1}{\sqrt{ } 2} \\ \frac{1}{\sqrt{ } 2} & \frac{1}{\sqrt{ } 2}\end{array}\right)\binom{p}{q}=\binom{3 \sqrt{ } 2}{4 \sqrt{ } 2}$ <br> $p-q=6$ and $p+q=8$ <br> or equivalent <br> $p=7$ and $q=1$ <br> both correct | M1 <br> M1 A1 <br> A1 <br> (4) |
|  | (c) Length of $O A(=$ length of $O B)=\sqrt{7^{2}+1^{2}},=\sqrt{50}=5 \sqrt{2}$ | M1, A1 |
|  | (d) $\mathrm{M}^{2}=\left(\begin{array}{cc}\frac{1}{\sqrt{ } 2} & -\frac{1}{\sqrt{ } 2} \\ \frac{1}{\sqrt{ } 2} & \frac{1}{\sqrt{ } 2}\end{array}\right)\left(\begin{array}{cc}\frac{1}{\sqrt{ } 2} & -\frac{1}{\sqrt{ } 2} \\ \frac{1}{\sqrt{ } 2} & \frac{1}{\sqrt{ } 2}\end{array}\right)=\left(\begin{array}{cc}0 & -1 \\ 1 & 0\end{array}\right)$ | M1 A1 (2) |
|  | (e) $\left(\begin{array}{cc}0 & -1 \\ 1 & 0\end{array}\right)\binom{3 \sqrt{2}}{4 \sqrt{2}}$ so coordinates are $(-4 \sqrt{ } 2,3 \sqrt{ } 2)$ | M1 A1 <br> (2) <br> [12] |
|  | Notes <br> Order of matrix multiplication needs to be correct to award Ms <br> (a) More than one transformation $0 / 2$ <br> (b) Second M1 for correct matrix multiplication to give two equations <br> Alternative: <br> (b) $\mathbf{M}^{-1}=\left(\begin{array}{cc}\frac{1}{\sqrt{ } 2} & \frac{1}{\sqrt{ } 2} \\ -\frac{1}{\sqrt{ } 2} & \frac{1}{\sqrt{ } 2}\end{array}\right)$ <br> First M1 A1 $\left(\begin{array}{cc} \frac{1}{\sqrt{ } 2} & \frac{1}{\sqrt{ } 2} \\ -\frac{1}{\sqrt{ } 2} & \frac{1}{\sqrt{ } 2} \end{array}\right)\binom{3 \sqrt{ } 2}{4 \sqrt{ } 2}=\binom{7}{1} \quad \text { Second M1 A1 }$ <br> (c) Correct use of their $p$ and their $q$ award M1 <br> (e) Accept column vector for final A1. |  |

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